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# THE EXACT SOLUTION OF THE PLANE ELASTICITY SECOND BASIC PROBLEM FOR THE SYMMETRIC AIRFOIL CRACKS.

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## Introduction.

The paper is the continuation of the paper [1], where the first and the mixed problems are solved. The singularity separation method is also used here, the boundary displacement being assumed to be differentiable.

## Analysis.

The elasticity second basic problem [2] for an unbounded domain  $D$  can be reduced to finding two functions analytic in

$D \setminus \{\infty\}$ :

$$f(z) = \Gamma z - \frac{X+iY}{2\pi(1+k)} \ln z + \frac{a}{z} + \dots, g(z) = \Gamma' z + \frac{k(X-iY)}{2\pi(1+k)} \ln z + \frac{a'}{z} + \dots, \quad (1)$$

$\Gamma, \Gamma', X+iY$  being known. The boundary condition is

$$\left\{ kf(z) - \overline{zf'(z)} - \overline{g(z)} \right\}_{|z=z(t)} = 2\mu(u(t) + iv(t)), \quad (2)$$

here  $z=z(t), t \in [0, 1]$ , is the equation of the boundary curve  $\partial D$ ,

$u'(t), v'(t)$  are assumed to be of Holder class.

We transfer to the function  $z(\zeta)$  which maps conformally  $E^- = \{\zeta =$